

경계 조건에 따른 자유 수면의 이상 거동

Y.J. Kim and S.B. Lee

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Problem statement

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Problem statement

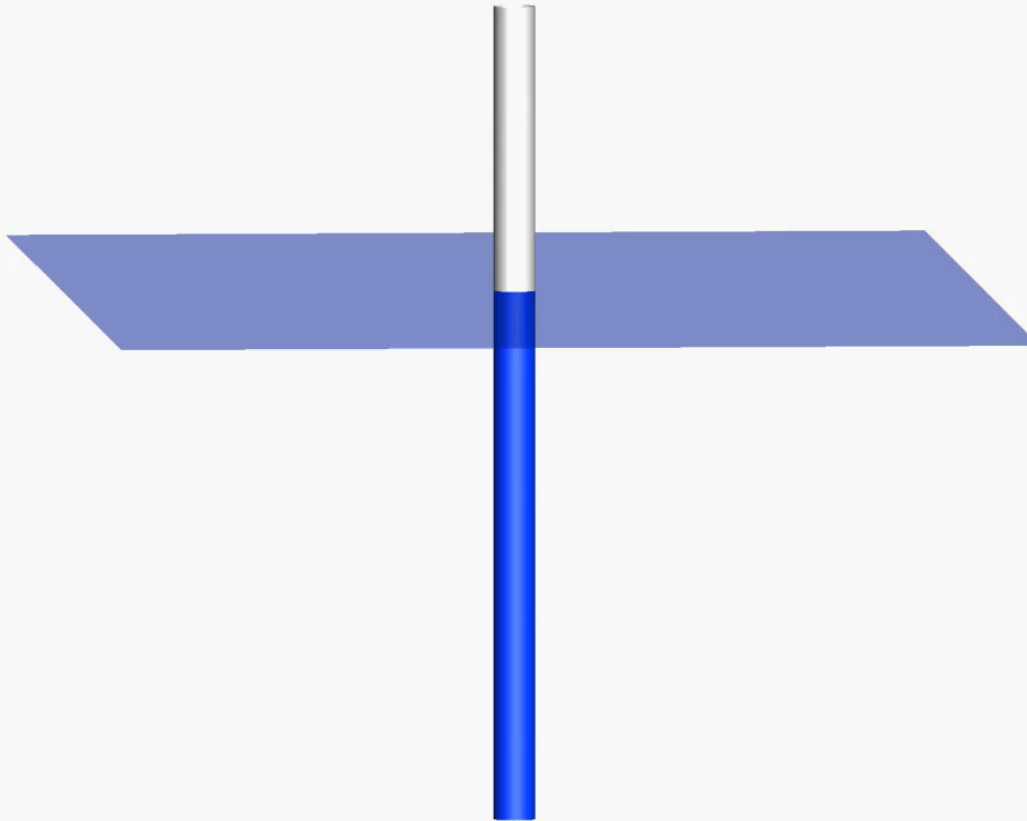
Simplification

Inherent effect of significant digit

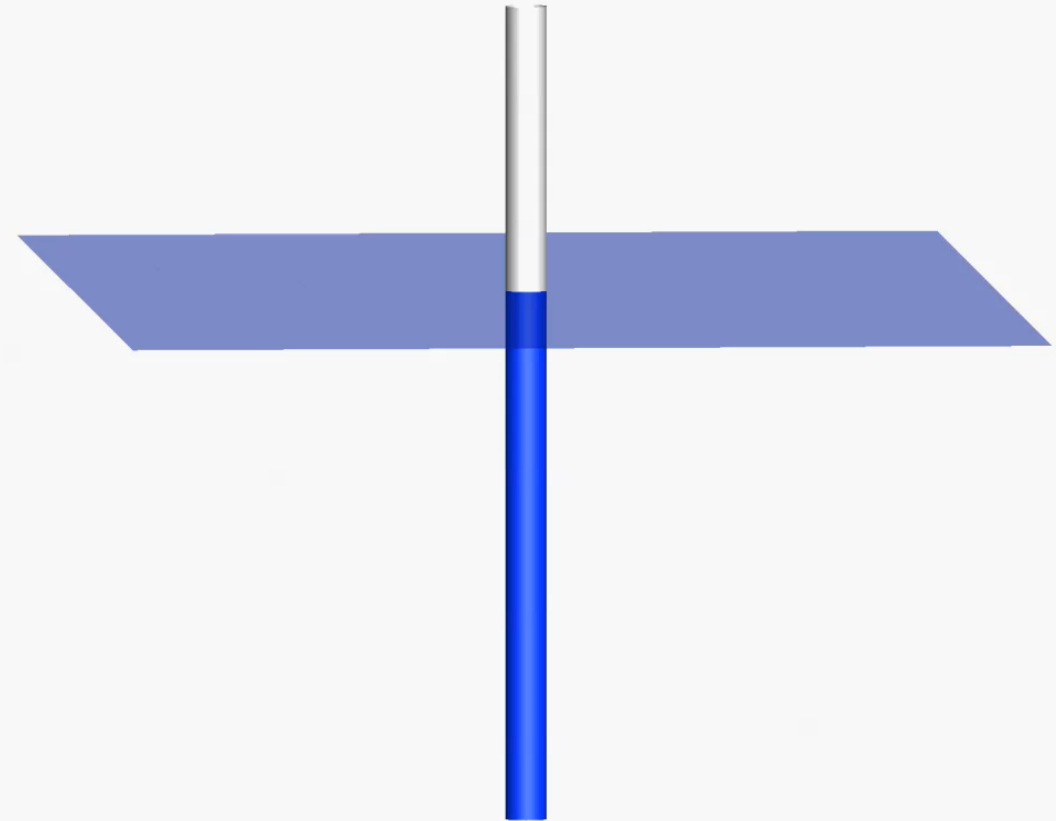
Code analysis

Visualization

(a) zeroGradient at all boundaries



(b) fixedValue at outlet boundary



- 경계 조건에 따른 자유 수면의 이상 거동 발생
- 이에 대한 원인 분석과 개선 필요

Simplification

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Problem statement

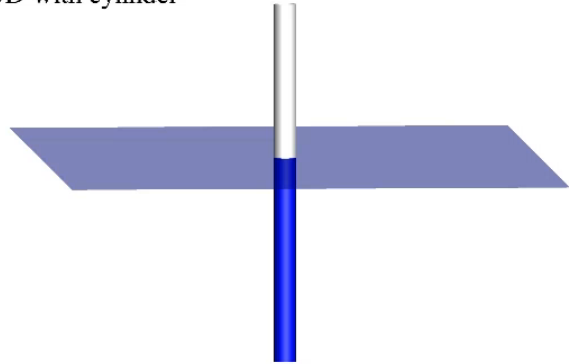
Simplification

Inherent effect of significant digit

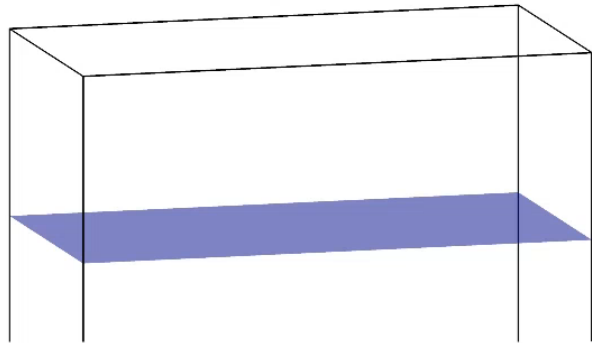
Code analysis

Visualization

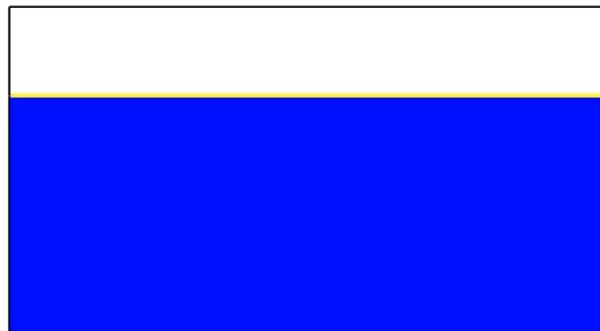
(a) 3D with cylinder



(b) 3D without cylinder



(c) 2D without cylinder



➤ 3D with cylinder case의 자유 수면 이상 거동

➤ 자유 수면의 이상 거동이 cylinder와 무관

➤ 2D without cylinder case에서 3D 결과와 동일 오류

Inherent effect of significant digit

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Problem statement

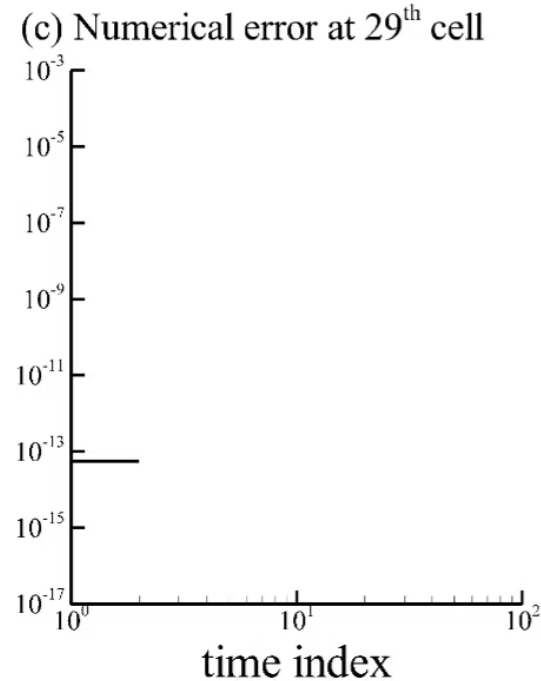
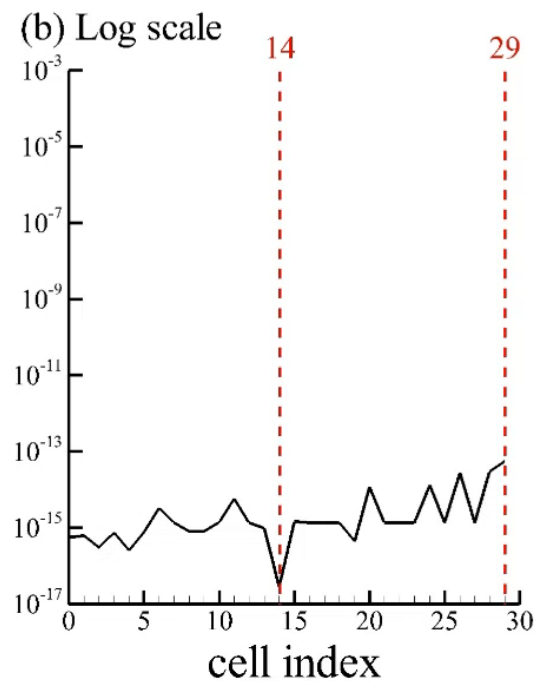
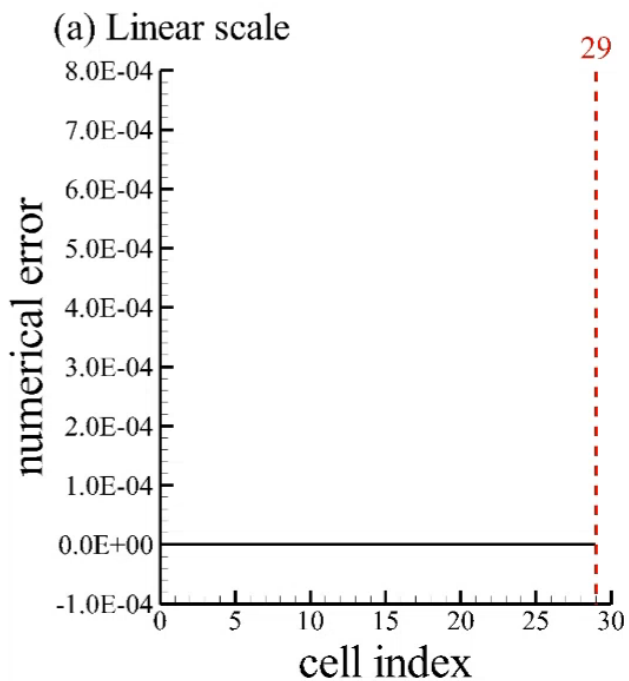
Simplification

Inherent effect of significant digit

Code analysis

Visualization

	zeroGradient		14
zeroGradient			zeroGradient
	zeroGradient		29



Inherent effect of significant digit

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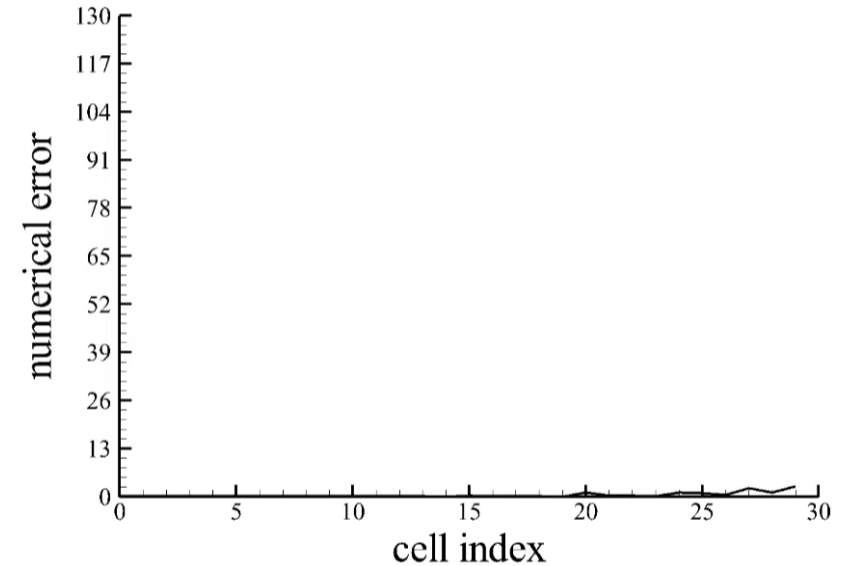
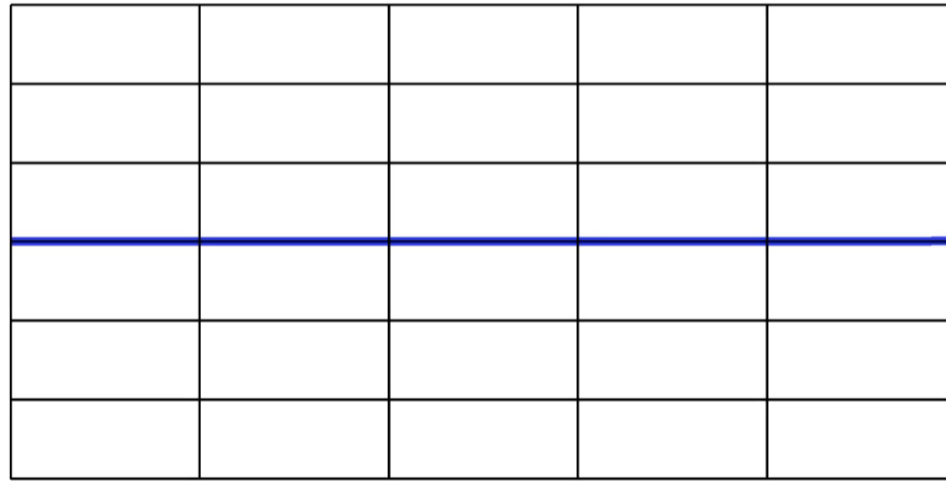
Problem statement

Simplification

Inherent effect of significant digit

Code analysis

Visualization



- ▶ double precision(10^{-15}) 이하의 수치 오차 누적
- ▶ 모든 경계에 zeroGradient 적용시 비 물리적 거동 발생
- ▶ 격자가 조밀한 경우, 자유 수면 이상 거동 지연

Inherent effect of significant digit

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Problem statement

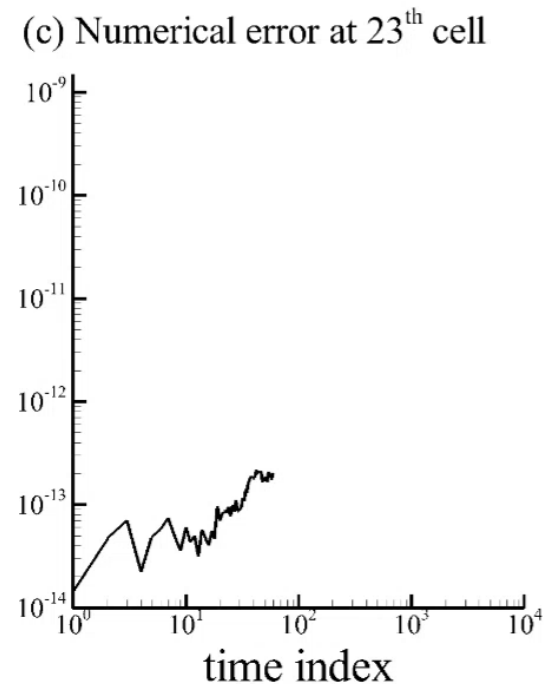
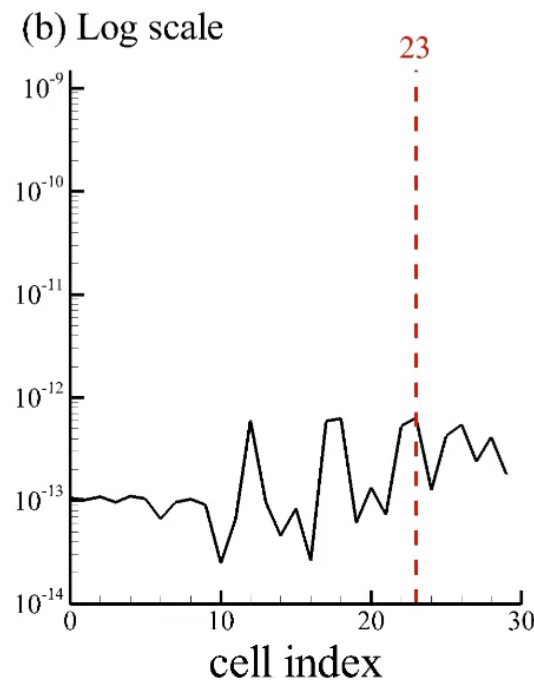
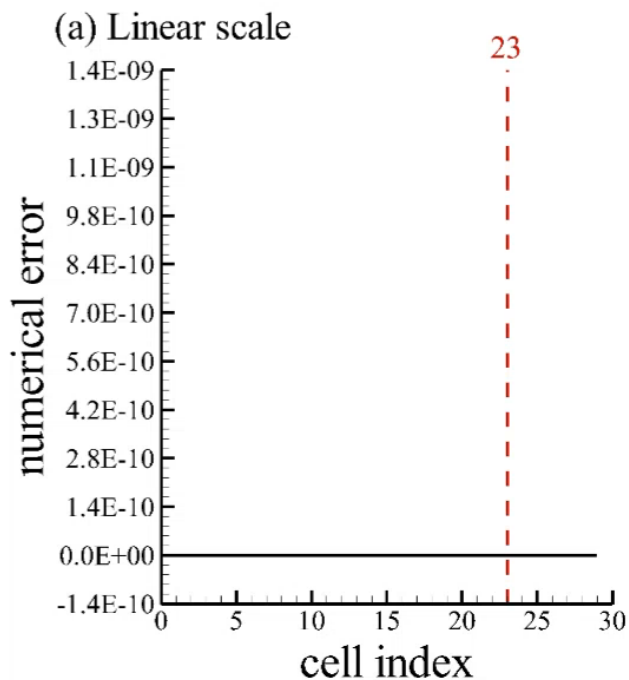
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Inherent effect of significant digit

Code analysis

Visualization

		zeroGradient		
zeroGradient				fixedValue
	23	zeroGradient		



Inherent effect of significant digit

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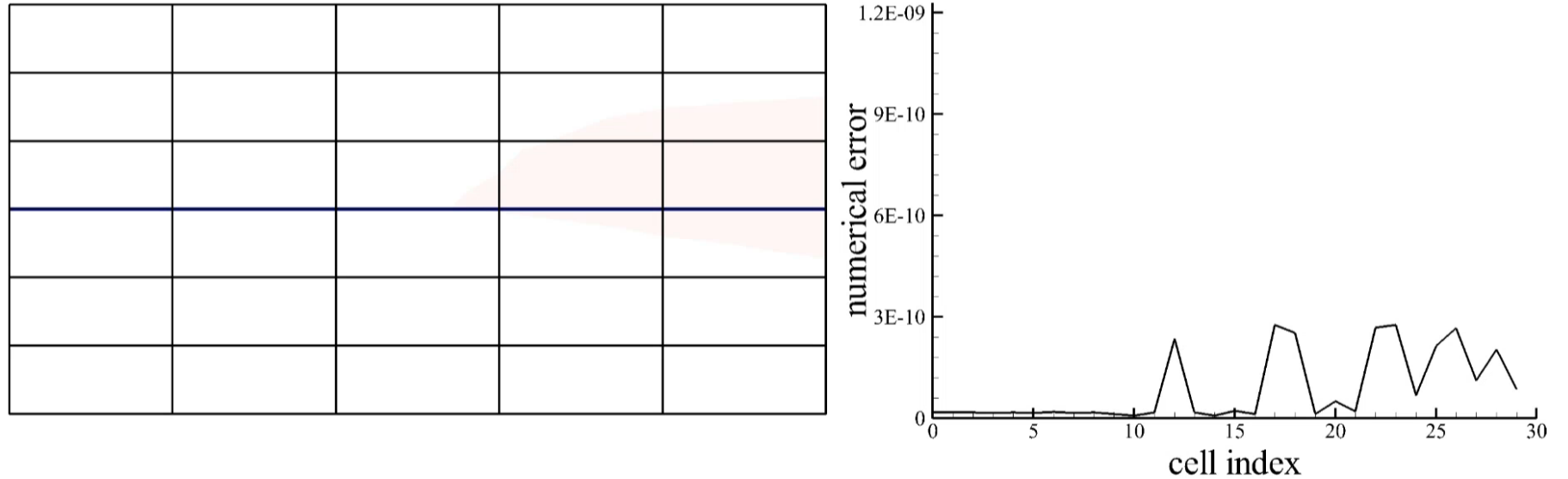
Problem statement

Simplification

Inherent effect of significant digit

Code analysis

Visualization



- ▶ 수치 오차가 10^{-9} 에 수렴
- ▶ Dirichlet 경계 조건이 수치 오차 제한
- ▶ 압력에 대한 `fixedValue` 경계 조건의 유효성 고찰 필요

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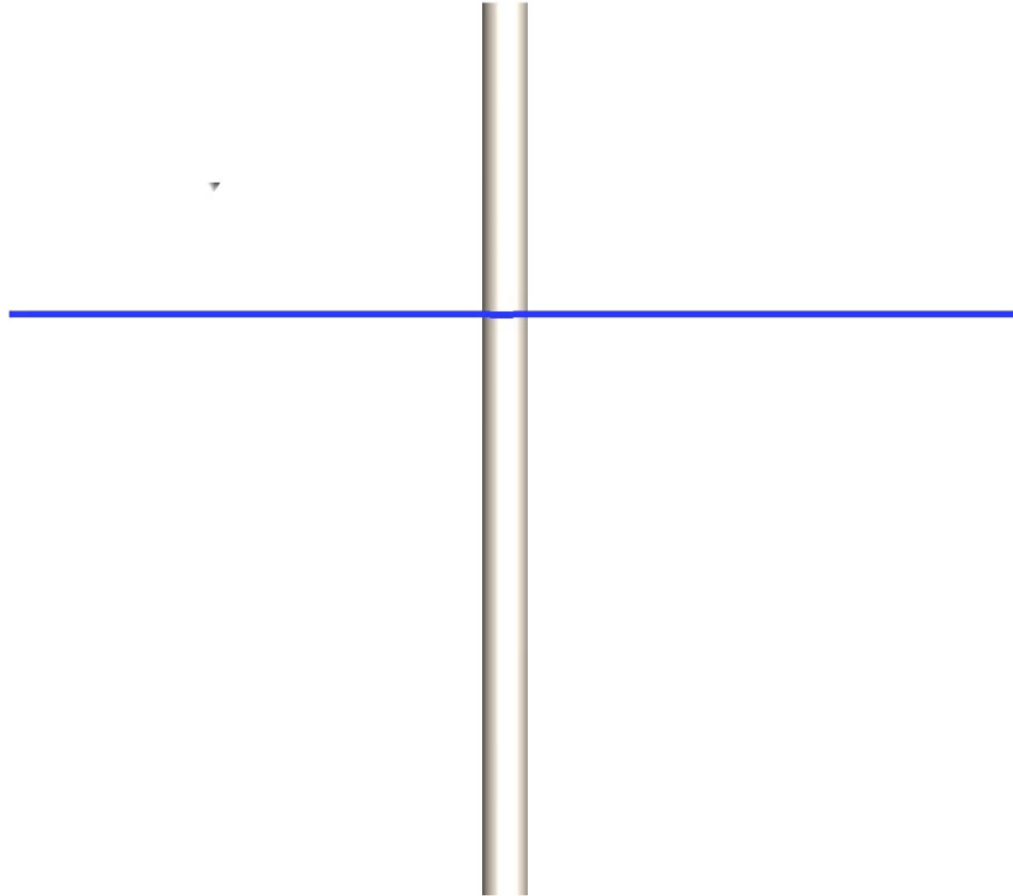
Simplification

Inherent effect of significant digit

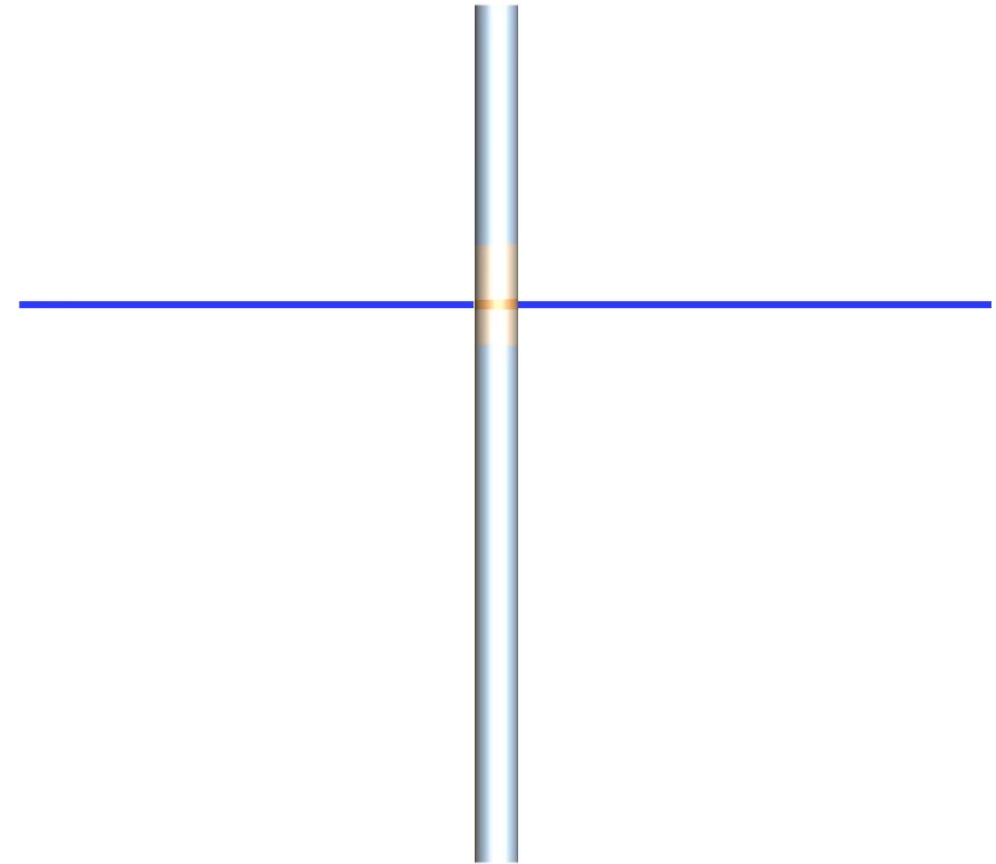
Code analysis

Visualization

(a) zeroGradient at all boundaries



(b) fixedValue at outlet boundary



➤ 2D simulation의 수치 오차가 3D with cylinder simulation에서도 발생함.

Code analysis

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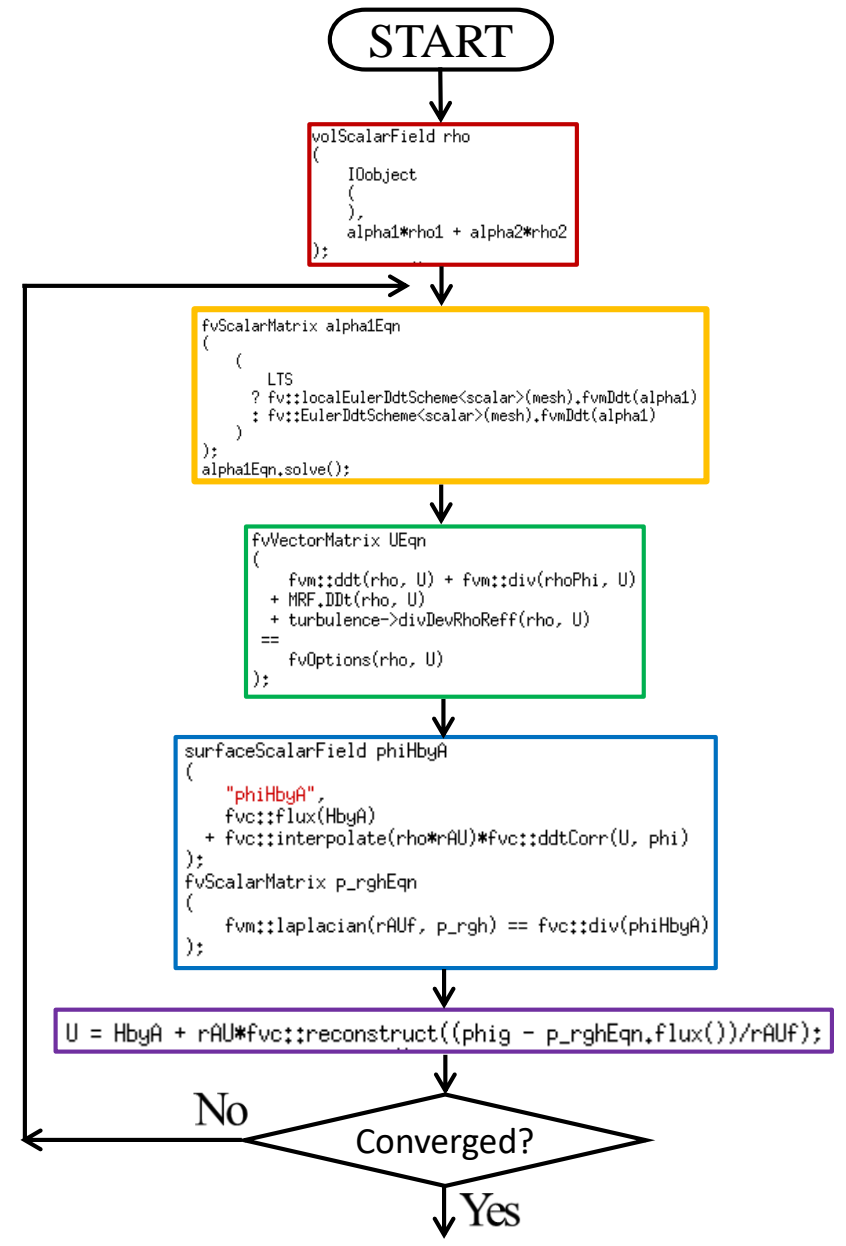
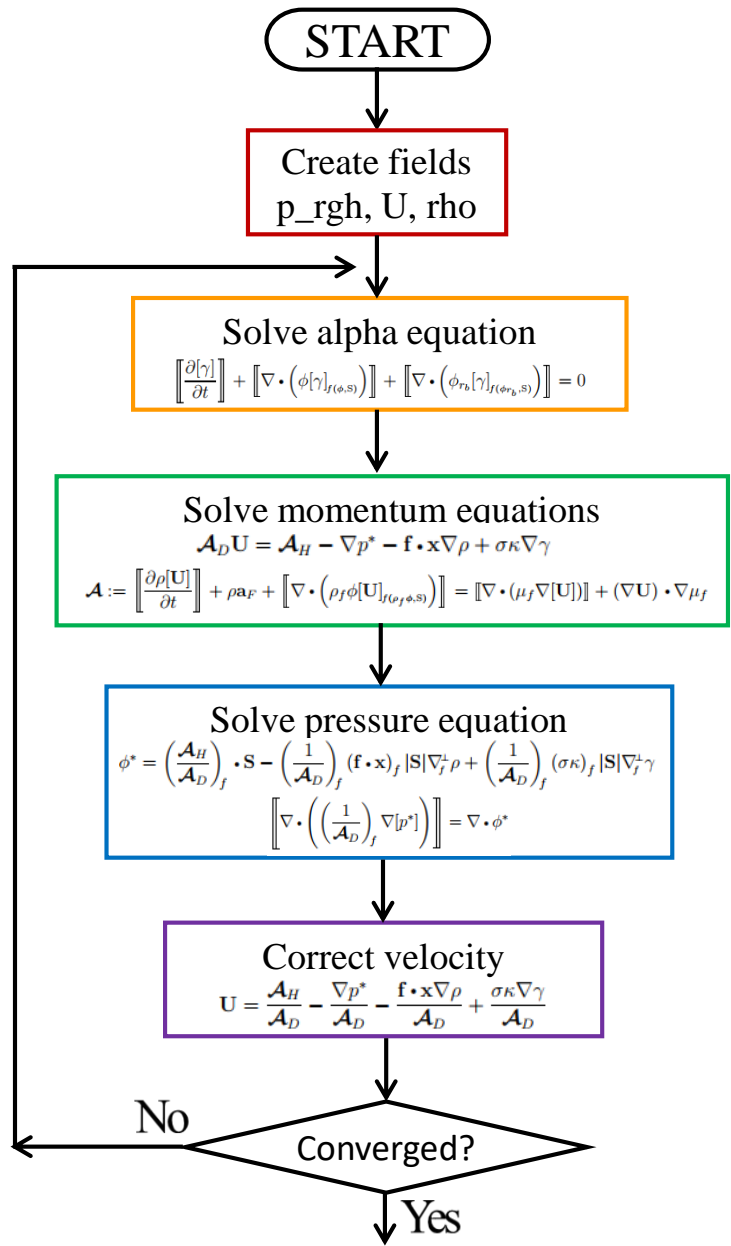
Problem statement

Simplification

Inherent effect of significant digit

Code analysis

Visualization



Code analysis

createFields.H

```

volScalarField p_rgh
(
    IOobject
    (
        "p_rgh",
        runTime.timeName(),
        mesh,
        IOobject::MUST_READ,
        IOobject::AUTO_WRITE
    ),
    mesh
);
    
```

```

volScalarField p
(
    IOobject
    (
        "p",
        runTime.timeName(),
        mesh,
        IOobject::NO_READ,
        IOobject::AUTO_WRITE
    ),
    p_rgh + rho*gh
);

label pRefCell = 0;
scalar pRefValue = 0.0;

setRefCell
(
    p,
    p_rgh,
    pimple.dict(),
    pRefCell,
    pRefValue
);

if (p_rgh.needReference())
{
    p += dimensionedScalar
    (
        "p",
        p.dimensions(),
        pRefValue - getRefCellValue(p, pRefCell)
    );
    p_rgh = p - rho*gh;
}
    
```

0	1	2	5	5	11	9	19	14
0		4		10		18		28
1	3	4	9	8	17	13	27	19
2		8		16		24		26
3	6	6	12	10	20	15	29	20
4		13		21		30		31
7	14	11	22	16	31	21	28	24
15		27		30		37		43
12	24	17	37	22	40	25	44	27
25		34		41		45		47
18	35	23	42	26	46	28	48	29

```

volScalarField rho
(
    IOobject
    (
        "rho",
        runTime.timeName(),
        mesh,
        IOobject::READ_IF_PRESENT
    ),
    alpha1*rho1 + alpha2*rho2
);
    
```

- rho1 : water(999.05)
- rho2 : air(1)
- alpha1 : water ratio
- alpha2 : 1-alpha1

celli	init_p_rgh[celli]
0	0.24524999999999968025576890795
1	0.24524999999999968025576890795
2	0.24524999999999968025576890795
3	0.24524999999999968025576890795
4	0.24524999999999968025576890795
5	0.24524999999999968025576890795
6	0.24524999999999968025576890795
7	0.24524999999999968025576890795
8	0.24524999999999968025576890795
9	0.24524999999999968025576890795
10	0.24524999999999968025576890795
11	0.24524999999999968025576890795
12	0.24524999999999968025576890795
13	0.24524999999999968025576890795
14	0.24524999999999968025576890795
15	0.24524999999999968025576890795
16	0.24524999999999968025576890795
17	0.24524999999999968025576890795
18	0.24524999999999968025576890795
19	0.24524999999999968025576890795
20	0.24524999999999968025576890795
21	0.24524999999999968025576890795
22	0.24524999999999968025576890795
23	0.24524999999999968025576890795
24	0.24524999999999968025576890795
25	0.24524999999999968025576890795
26	0.24524999999999968025576890795
27	0.24524999999999968025576890795
28	0.24524999999999968025576890795
29	0.24524999999999968025576890795

celli	init_rho[celli]
0	1
1	1
2	1
3	1
4	1
5	1
6	1
7	999.049999999999999840838427189738
8	1
9	1
10	1
11	999.049999999999999840838427189738
12	999.049999999999999840838427189738
13	1
14	1
15	1
16	999.049999999999999840838427189738
17	999.049999999999999840838427189738
18	999.049999999999999840838427189738
19	1
20	1
21	999.049999999999999840838427189738
22	999.049999999999999840838427189738
23	999.049999999999999840838427189738
24	999.049999999999999840838427189738
25	999.049999999999999840838427189738
26	999.049999999999999840838427189738
27	999.049999999999999840838427189738
28	999.049999999999999840838427189738
29	999.049999999999999840838427189738

1) $p_rgh = 0.0$

2) $p = p_rgh + rgh$
 -> value of each rho & cell center

3) $p -= pRefValue(C_{14})$
 (pRefValue = $1 \times 9.81 \times 0.025 = -0.24525$)

4) $p_rgh = p - rgh$

$\Rightarrow p_rgh = p_rgh + rgh - pRefValue - rgh$

$\Rightarrow p_rgh -= pRefValue$

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UEqn.H

```
MRF.correctBoundaryVelocity(U);

fvVectorMatrix UEqn
(
    fvm::ddt(rho, U) + fvm::div(rhoPhi, U)
    + MRF.DDt(rho, U)
    + turbulence->divDevRhoReff(rho, U)
    ==
    fvOptions(rho, U)
);

UEqn.relax();

fvOptions.constrain(UEqn);

if (pimple.momentumPredictor())
{
    solve
    (
        UEqn
        ==
        fvc::reconstruct_DAU
        (
            mixture.surfaceTensionForce()
            - ghf*fvc::snGrad(rho)
            - fvc::snGrad(p_rgh)
            ) * mesh.magSf()
        );
    fvOptions.correct(U);
}
```

UEqn == reconstruct

```
template<class Type>
tmp<GeometricField<Type, fvsPatchField, surfaceMesh>>
snGradScheme<Type>::snGrad
(
    const GeometricField<Type, fvPatchField, volMesh>& vf
) const
{
    tmp<GeometricField<Type, fvsPatchField, surfaceMesh>> tsf
    (
        snGrad(vf, deltaCoeffs(vf))
    );
    if (corrected())
    {
        tsf.ref() += correction(vf);
    }
    return tsf;
}
```

UEqn.source()

```
0 (2.8024666666666644293507207331e-06 0 0)
1 (2.8024666666666644293507207331e-06 0 0)
2 (2.39999999999999989139546838213e-06 0 0)
3 (2.8024666666666644293507207331e-06 0 0)
4 (2.39999999999999989139546838213e-06 0 0)
5 (2.399999999999999862084604750068e-06 0 0)
6 (2.40000000000000031491194200928e-06 0 0)
7 (0.00279752981949999996597044926716 0 0)
8 (2.39999999999999904436252112783e-06 0 0)
9 (2.40000000000000031491194200928e-06 0 0)
10 (2.39999999999999904436252112783e-06 0 0)
11 (0.002397720000000003198008524663 0 0)
12 (0.00279752981950000039965131826136 0 0)
13 (2.400000000000000158546136289073e-06 0 0)
14 (2.3999999999999977381310024638e-06 0 0)
15 (2.40000000000000031491194200928e-06 0 0)
16 (0.002397719999999994524391144779 0 0)
17 (0.002397720000000003198008524663 0 0)
18 (0.00279752981949999996597044926716 0 0)
19 (2.39999999999999904436252112783e-06 0 0)
20 (2.39999999999999862084604750068e-06 0 0)
21 (0.002397720000000003198008524663 0 0)
22 (0.00239771999999999858507737648949 0 0)
23 (0.002397719999999994524391144779 0 0)
24 (0.002397719999999994524391144779 0 0)
25 (0.002397720000000003198008524663 0 0)
26 (0.0023977199999999858507737648949 0 0)
27 (0.0023977199999999815139650749529 0 0)
28 (0.002397720000000003198008524663 0 0)
29 (0.0023977199999999858507737648949 0 0)
```

```
template<class Type>
tmp<GeometricField<Type, fvsPatchField, surfaceMesh>>
snGradScheme<Type>::snGrad
(
    const GeometricField<Type, fvPatchField, volMesh>& vf,
    const tmp<surfaceScalarField>& tdeltaCoeffs,
    const word& snGradName
)
{
    :
    forAll(owner, facei)
    {
        ssf[facei] =
            deltaCoeffs[facei]*(vf[neighbour[facei]] - vf[owner[facei]]);
    }
}
```

```
template<>
Foam::tmp<Foam::surfaceScalarField>
Foam::fvc::correctedSnGrad<Foam::scalar>::correction
(
    const volScalarField& vsf
) const
{
    return fullGradCorrection(vsf);
}
```

```
0 (2.8024666666666644293507207331e-06 0 0)
1 (2.8024666666666644293507207331e-06 0 0)
2 (2.39999999999999989139546838213e-06 0 0)
3 (2.80246666666666658502323139455e-06 -1.59872115546022545871233633251e-20 0)
4 (2.39999999999999989139546838213e-06 0 0)
5 (2.399999999999999862084604750068e-06 0 0)
6 (2.40000000000000031491194200928e-06 -1.59872115546022636149199776403e-20 0)
7 (0.00279752981949999996597044926716 -1.59872115546022545871233633251e-20 0)
8 (2.39999999999999904436252112783e-06 0 0)
9 (2.40000000000000031491194200928e-06 0 0)
10 (2.40000000000002022018620248534e-06 -1.59872115546022515778578252201e-20 0)
11 (0.002397720000000003198008524663 -1.59872115546022636149199776403e-20 0)
12 (0.00279752981950000039965131826136 2.67664290731772667483648855024e-19 0)
13 (2.400000000000000158546136289073e-06 0 0)
14 (2.3999999999999977381310024638e-06 0 0)
15 (2.40000000000001090282378268803e-06 -1.59872115546022515778578252201e-20 0)
16 (0.002397719999999994524391144779 -1.59872115546022515778578252201e-20 0)
17 (0.002397720000000003198008524663 -2.67664290731772619335400245343e-19 0)
18 (0.00279752981949999996597044926716 2.67664290731772619335400245343e-19 0)
19 (2.39999999999999904436252112783e-06 0 0)
20 (2.3999999999999862084604750068e-06 -1.598721155460224856892287115e-20 0)
21 (0.002397720000000003198008524663 -1.59872115546022515778578252201e-20 0)
22 (0.00239771999999999858507737648949 -2.67664290731772715631897464705e-19 0)
23 (0.002397719999999994524391144779 -2.6766429073177253038903025982e-19 0)
24 (0.002397719999999994524391144779 -1.59872115546022515778578252201e-20 0)
25 (0.002397720000000003198008524663 1.18083579715242361463252236736e-34 0)
26 (0.0023977199999999858507737648949 -2.67664290731772715631897464705e-19 0)
27 (0.0023977199999999815139650749529 0 0)
28 (0.002397720000000003198008524663 1.18083579715242382845639917474e-34 0)
29 (0.0023977199999999858507737648949 0 0)
```

Code analysis

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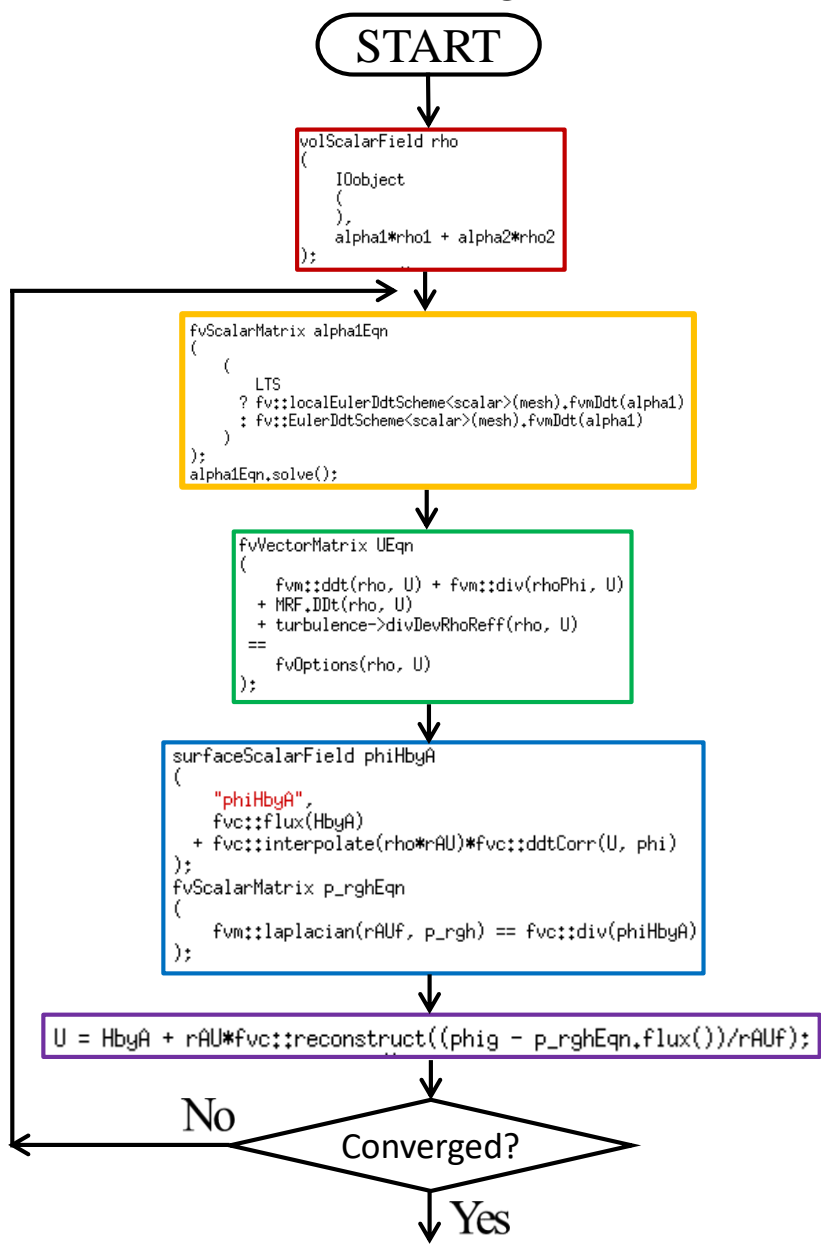
Problem statement

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pEqn.H

```

volScalarField rAU("rAU", 1.0/UEqn.A());
surfaceScalarField rAUf("rAUf", fvc::interpolate(rAU));
volVectorField HbyA(constrainHbyA(rAU*UEqn.H(), U, p_rgh));
surfaceScalarField phiHbyA
(
  "phiHbyA",
  fvc::flux(HbyA)
  + fvc::interpolate(rho*rAU)*fvc::ddtCorr(U, phi)
);
MRF.makeRelative(phiHbyA);
adjustPhi(phiHbyA, U, p_rgh);
surfaceScalarField phig
(
  (
    mixture.surfaceTensionForce()
    - ghf*fvc::snGrad(rho)
  ) * rAUf * mesh.magSf()
);
phiHbyA += phig;
// Update the pressure BCs to ensure flux consistency
constrainPressure(p_rgh, U, phiHbyA, rAUf, MRF);
while (pimple.correctNonOrthogonal())
{
  fvScalarMatrix p_rghEqn
  (
    fvm::laplacian(rAUf, p_rgh) == fvc::div(phiHbyA)
  );
  p_rghEqn.setReference(pRefCell, getRefCellValue(p_rgh, pRefCell));
  p_rghEqn.solve(mesh.solver(p_rgh.select(pimple.finalInnerIter())));
  if (pimple.finalNonOrthogonalIter())
  {
    phi = phiHbyA - p_rghEqn.flux();
    p_rgh.relax();
    U = HbyA + rAU*fvc::reconstruct((phig - p_rghEqn.flux())/rAUf);
    U.correctBoundaryConditions();
    fvOptions.correct(U);
  }
}
#include "continuityErrs.H"
p == p_rgh + rho*gh;
if (p_rgh.needReference())
{
  p += dimensionedScalar
  (
    "p",
    p.dimensions(),
    pRefValue - getRefCellValue(p, pRefCell)
  );
  p_rgh = p - rho*gh;
}
  
```

$$rAU = \frac{1}{UEqn.A()} = \frac{mesh.V()}{UCoeff.Diag()}$$

$$HbyA = rAU \times \frac{(source-coeff \times phi')}{mesh.V()} = \frac{(source-coeff \times phi')}{UCoeff.Diag()}$$

$$phig = rAUf \times UEqn.snGrad(rho)$$

p_rghEqn.flux()

```

for (label face=0; face<l.size(); face++)
{
  faceHpsi[face] =
    Upper[face]*psi[u[face]]
    - Lower[face]*psi[l[face]];
}
  
```

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UEqn.H

```
MRF.correctBoundaryVelocity(U);

fvVectorMatrix UEqn
(
    fvm::ddt(rho, U) + fvm::div(rhoPhi, U)
    + MRF.DDt(rho, U)
    + turbulence->divDevRhoReff(rho, U)
    ==
    fvOptions(rho, U)
);

UEqn.relax();

fvOptions.constrain(UEqn);

if (pimple.momentumPredictor())
{
    solve
    (
        UEqn
        ==
        fvc::reconstruct_DAU
        (
            (
                mixture.surfaceTensionForce()
                - ghf*fvc::snGrad(rho)
                - fvc::snGrad(p_rgh)
            ) * mesh.magSf()
        )
    );

    fvOptions.correct(U);
}
```

pEqn.H

```
volScalarField rAU("rAU", 1.0/UEqn.A());
surfaceScalarField rAUF("rAUF", fvc::interpolate(rAU));

volVectorField HbyA(constrainHbyA(rAU*UEqn.H(), U, p_rgh));

surfaceScalarField phiHbyA
(
    "phiHbyA",
    fvc::flux(HbyA)
    + fvc::interpolate(rho*rAU)*fvc::ddtCorr(U, phi)
);
MRF.makeRelative(phiHbyA);
adjustPhi(phiHbyA, U, p_rgh);

surfaceScalarField phig
(
    (
        mixture.surfaceTensionForce()
        - ghf*fvc::snGrad(rho)
        ) * rAUF * mesh.magSf()
);

phiHbyA += phig;

// Update the pressure BCs to ensure flux consistency
constrainPressure(p_rgh, U, phiHbyA, rAUF, MRF);

while (pimple.correctNonOrthogonal())
{
    fvScalarMatrix p_rghEqn
    (
        fvm::laplacian(rAUF, p_rgh) == fvc::div(phiHbyA)
    );

    p_rghEqn.setReference(pRefCell, getRefCellValue(p_rgh, pRefCell));
    p_rghEqn.solve(mesh.solver(p_rgh.select(pimple.finalInnerIter())));

    if (pimple.finalNonOrthogonalIter())
    {
        phi = phiHbyA - p_rghEqn.flux();

        p_rgh.relax();

        U = HbyA + rAU*fvc::reconstruct((phi - p_rghEqn.flux())/rAUF);
        U.correctBoundaryConditions();
        fvOptions.correct(U);
    }
}

#include "continuityErrs.H"

p == p_rgh + rho*gh;

if (p_rgh.needReference())
{
    p += dimensionedScalar
    (
        "p",
        p.dimensions(),
        pRefValue - getRefCellValue(p, pRefCell)
    );
    p_rgh = p - rho*gh;
}
```

$$U_{Error} = U - U_{init}$$

$$p_rgh_{Error} = p_rgh - p_rgh_{init}$$

